



**Auburn University**  
*Samuel Ginn College of Engineering*

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# **Product Life-Cycle Management and Decision Support Models for Area-Array Electronics in Extreme Environments**

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# Objective

Development of a tool which can be used for appropriate selection and deployment of area-array packages in harsh environments.



# Motivation

Scarcity of models for turn key approach, for making trade-offs between geometry and materials and quantitatively evaluating the impact on reliability.

Component Obsolescence, multiple suppliers, product platforms, die shrink, and underfills.

Existing standards, publications do not address a complete set of system-level material and design parameters.

First-order models typically address single effects only.



## State-of-Art

Previous studies have shown the,

Effect of material and geometric parameters on reliability of flip-chip on organic laminate printed circuit boards [Yeh et al., 1996, Popelar, 1998].

2-D analysis of geometry and architecture parameters for trade-off studies [Lu 2000].

Non-linear finite element models [Darveaux 1996, Gustafsson 2000, Lall 2004]

First-order closed form models [Engelmaier 1984, Clech 1996, Vandeveld 1998].



# Scope of the Guidelines

Aid for understanding the sensitivity of component reliability to geometry, package architecture, material properties and board attributes.

Tool for doing trade-offs between geometry, materials and quantitatively evaluating the impact on reliability.

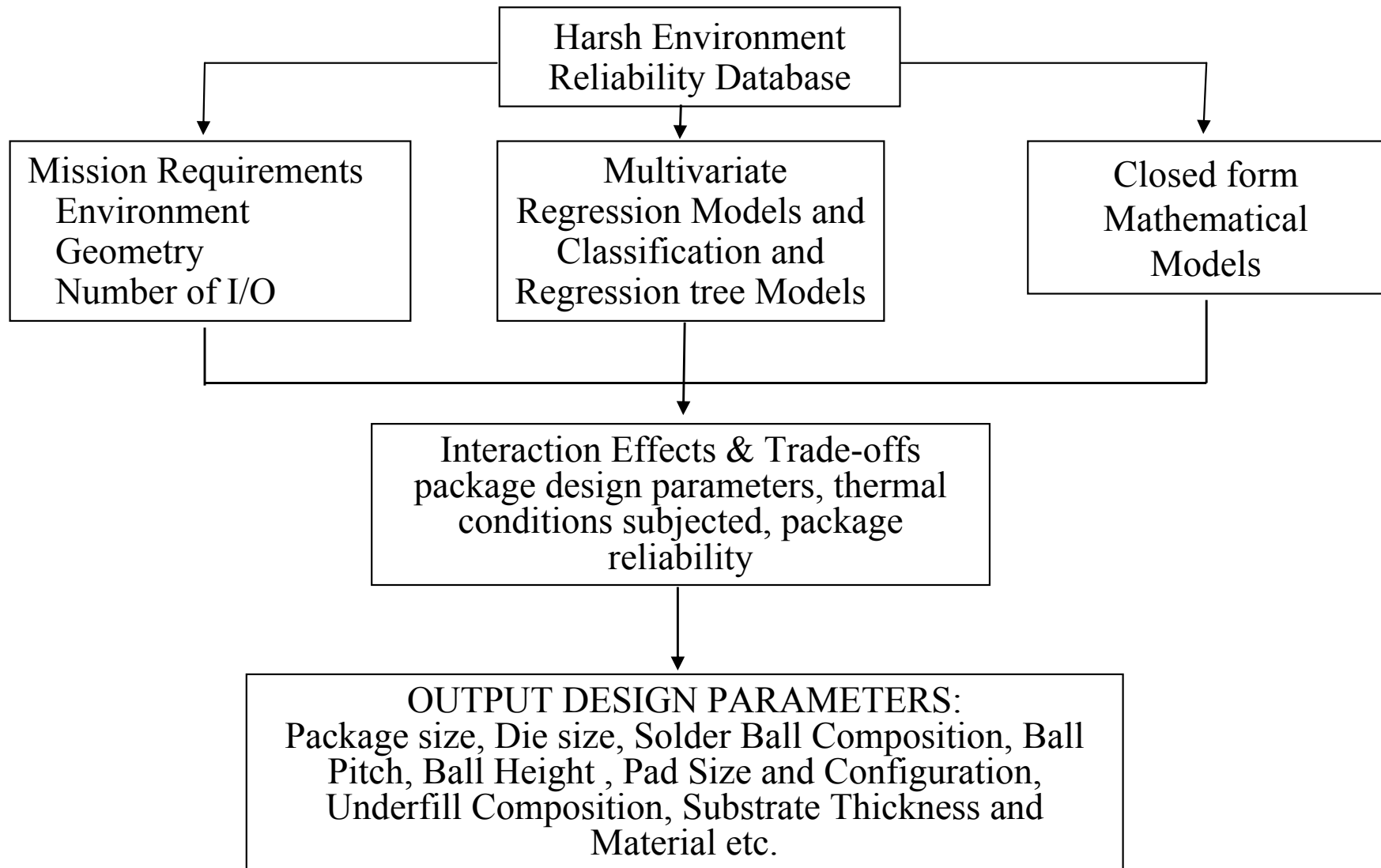
Does NOT specify –

The required level of component reliability for use in various mission critical applications.

A comprehensive library of every component that can be used in harsh environments.



# Structure

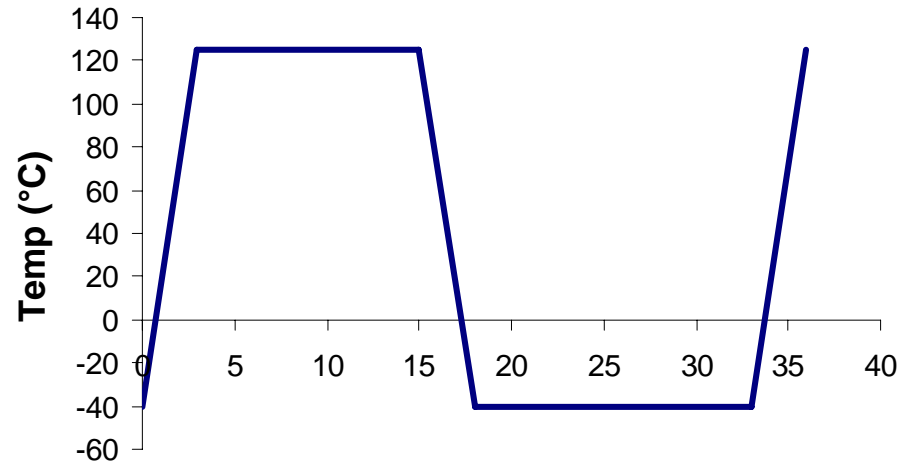




# Thermal Profiles

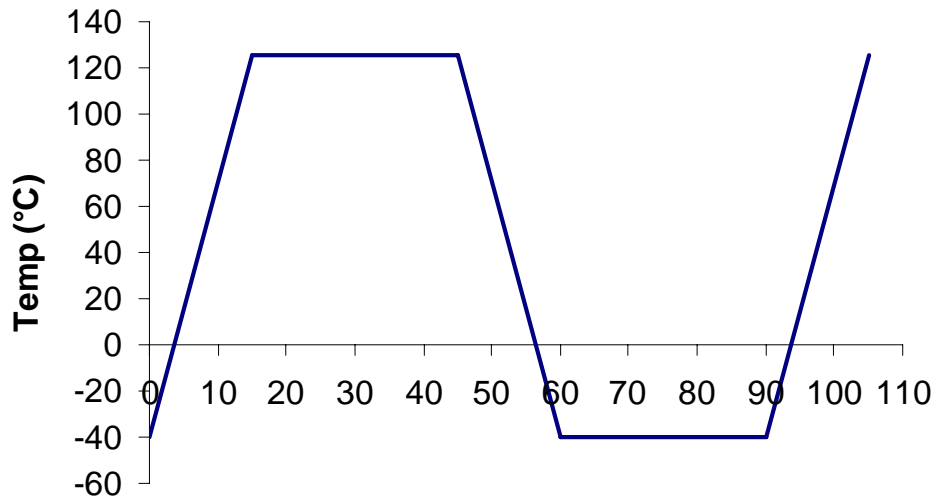
- 40°C to 125°C, 3min ramp, 12min dwell
- 40°C to 125°C, 15min ramp, 15min dwell
- 40°C to 125°C, 15min ramp, 30min dwell
- 0°C to 100°C, 30min ramp, 30min dwell
- 55 to 125 °C, 6 c/h, 5 min dwell

-40°C  $\Leftrightarrow$  125°C, 3min ramp, 12min dwell



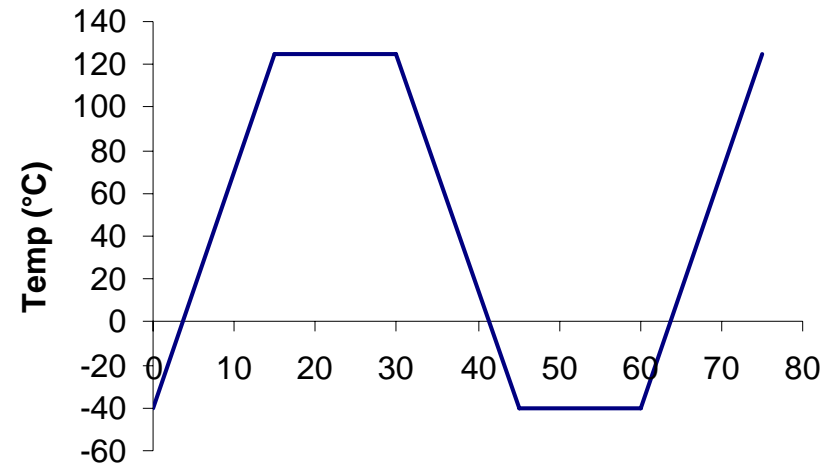
Time (mins)

-40°C  $\Leftrightarrow$  125°C, 15min ramp, 30min dwell



Time (mins)

-40°C  $\Leftrightarrow$  125°C, 15min ramp, 15min dwell



Time (mins)



# Scope of Accelerated Test Database

## > *FlexBGA, PBGA*

|                | <b>FlexBGA</b>      | <b>PBGA</b>      |
|----------------|---------------------|------------------|
| Package Size   | 7.5mm to 27mm       | 15mm to 27mm     |
| Number of I/O  | 40 to 381           | 132 to 324       |
| Die Size       | 3.5mm to 11.5mm     | 6.8mm to 10mm    |
| Ball Diameter  | 0.3mm - 0.5mm       | 0.5mm to 0.8mm   |
| Ball Pitch     | 0.5mm, 0.8mm, 1.0mm | 1.0mm, 1.27mm    |
| PCB type       | 4 Layer FR-4        | 4 Layer FR-4     |
| PCB thickness  | 0.85mm, 1.6mm       | 1.6mm            |
| Surface Finish | OSP, HASL, Ni/Au    | OSP, HASL, Ni/Au |





# Scope of Accelerated Test Database

## > *Flip-Chip*

|                                      | <b>Flip-Chip</b>   |
|--------------------------------------|--|
| Die Size                             | 3 mm to 12.6 mm  |
| Ball Count                           | 42 to 184  |
| Ball Pitch                           | 0.2 mm to 0.457 mm   |
| Ball Diameter                        | 0.04 mm to 0.195 mm  |
| Ball Height                          | 0.04 mm to 0.147 mm  |
| Solder Composition                   | Sn63Pb37, Sn96.5Ag3.5,<br>95.5Sn3.5Ag1.0Cu, Sn99.3Cu0.7,<br>Sn95.8Ag3.5Cu0.7 |
| PCB Thickness                        | 0.5 mm to 1 mm   |
| T <sub>High</sub> , Accelerated Test | 100°C, 125°C, 150°C  |
| T <sub>Low</sub> , Accelerated Test  | -55°C, -40°C, 0°C  |



# Stepwise Regression

For each variable added, test to see if any previously selected variable may be deleted without appreciable loss of explanatory power.

$$\psi \subset \{1, 2, 3, \dots, p\}$$

Select subset,  $q \leq p$ , candidate variables

$$F_{\psi} = a + \sum_{k \in \psi} b_k x_k$$

where  $a$  and  $b_k$  ( $k \in \psi$ ) are estimated using method of least squares.

| Step               | 1      | 2      | 3      | 4      | 5     | 6      | 7      |
|--------------------|--------|--------|--------|--------|-------|--------|--------|
| Constant           | 2494.3 | 1783.9 | 2669.1 | 1088.2 | 910.2 | 3080.6 | 4438.8 |
| DieLengthMM        | -147   | -115   | -87    | -87    | -296  | -543   | -665   |
| T-Statistic        | -3.24  | -2.59  | -2.13  | -2.30  | -2.23 | -3.59  | -4.03  |
| P-Value            | 0.002  | 0.013  | 0.039  | 0.026  | 0.031 | 0.001  | 0.000  |
| UnderfillEGpa      |        | 56     | 136    | 158    | 144   | 128    | 110    |
| T-Statistic        |        | 2.53   | 4.42   | 5.37   | 4.77  | 4.46   | 3.67   |
| P-Value            |        | 0.015  | 0.000  | 0.000  | 0.000 | 0.000  | 0.001  |
| BallPitchMM        |        |        | -6555  | -8877  | -8351 | -7227  | -6925  |
| T-Statistic        |        |        | -3.41  | -4.56  | -4.31 | -3.93  | -3.83  |
| P-Value            |        |        | 0.001  | 0.000  | 0.000 | 0.000  | 0.000  |
| BallDiaMM          |        |        |        | 22923  | 29754 | 31895  | 32913  |
| T-Statistic        |        |        |        | 2.94   | 3.41  | 3.93   | 4.13   |
| P-Value            |        |        |        | 0.005  | 0.001 | 0.000  | 0.000  |
| UndercoverAreaSqMM |        |        |        |        | 19    | 43     | 53     |
| T-Statistic        |        |        |        |        | 1.63  | 3.16   | 3.63   |
| P-Value            |        |        |        |        | 0.110 | 0.003  | 0.001  |
| BallHeightMM       |        |        |        |        |       | -19650 | -18387 |
| T-Statistic        |        |        |        |        |       | -2.83  | -2.69  |
| P-Value            |        |        |        |        |       | 0.007  | 0.010  |
| DeltaT             |        |        |        |        |       |        | -6.9   |
| T-Statistic        |        |        |        |        |       |        | -1.67  |
| P-Value            |        |        |        |        |       |        | 0.102  |
| S                  | 1055   | 999    | 900    | 832    | 817   | 757    | 742    |
| R-Sq               | 18.28  | 28.27  | 43.00  | 52.37  | 55.16 | 62.33  | 64.74  |
| R-Sq(Adj)          | 16.54  | 25.16  | 39.20  | 48.04  | 49.94 | 56.94  | 58.72  |
| C-P                | 46.5   | 37.3   | 22.8   | 14.3   | 13.2  | 7.2    | 6.5    |



# Multivariate Regression

Linear :

$$t_{63.2\%} = a_0 + \sum_{k=1}^n b_k f_k$$

Log :

$$t_{63.2\%} = a_0 \prod_{k=1}^n (f_k)^{b_k}$$



# Log Multivariate Regression Models > *FlexBGA*

## MULTIVARIATE REGRESSION MODEL OF FLEX-SUBSTRATE BGA THERMAL FATIGUE DATA

| Predictor   | Coefficient and Indices<br>(Log A, $b_n$ ) | SE Coeff | T      | p     |
|---|--|----------|--------|-------|
| LogConstant (or Log A)                            | 3.8066                                     | 0.7513   | 5.07   | 0.000 |
| LogDietoBodyRatio                                 | -1.7395                                    | 0.1532   | -11.35 | 0.000 |
| LogBallCount                                      | 0.41623                                    | 0.08347  | 4.99   | 0.000 |
| LogBallDiaMM                                      | 0.9485                                     | 0.2779   | 3.41   | 0.002 |
| LogPCBthkMM                                       | -0.5322                                    | 0.1105   | -4.82  | 0.000 |
| LogEMCFillID                                      | 0.19127                                    | 0.0434   | 4.41   | 0.000 |
| LogMasfDefID                                      | 0.25762                                    | 0.06285  | 4.10   | 0.000 |
| LogBoardFinishID                                  | -0.07794                                   | 0.04044  | -1.93  | 0.061 |
| LogDeltaT   | -0.9453                                    | 0.2789   | -3.39  | 0.002 |
| S = 0.0946    R-Sq = 90.20%    R-Sq(adj) = 88.20% |  |          |        |       |



# Log Multivariate Regression Models

## > *Flip-Chip*

| Predictors<br>( $\ln a_0, f_k$ ) | Coeff<br>( $b_k$ ) | SE<br>Coeff | T      | P-Value |
|----------------------------------|--------------------|-------------|--------|---------|
| Constant ( $\ln a_0$ )           | 66.924             | 19.565      | 3.421  | 0.002   |
| $\ln \text{UndCovSqmm}$          | 34.088             | 10.841      | 3.144  | 0.004   |
| $\ln \text{UndEGpa}$             | 0.481              | 0.219       | 2.195  | 0.035   |
| $\ln \text{UndCTEppm}$           | -0.292             | 0.102       | -2.862 | 0.007   |
| $\ln \text{SolderEGpa}$          | -0.665             | 0.283       | -2.352 | 0.025   |
| $\ln \text{SolderDiaMM}$         | 1.805              | 0.867       | 2.082  | 0.045   |
| $\ln \text{DeltaTdegC}$          | -4.813             | 2.342       | -2.055 | 0.048   |
| $\ln \text{PitchMM}$             | -0.800             | 0.366       | -2.184 | 0.036   |
| $\ln \text{BallHgtMM}$           | 2.645              | 0.794       | 3.331  | 0.002   |
| $\ln \text{DiagLenMM}$           | -68.216            | 21.645      | -3.152 | 0.003   |



# Linear Multivariate Regression Models

## > *Flip-Chip*

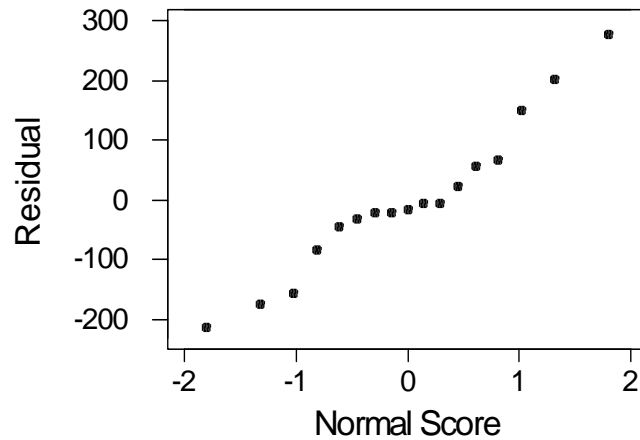
| Predictors<br>( $a_0, f_k$ ) | Coeff<br>( $b_k$ ) | SE<br>Coeff | T      | P-Value |
|------------------------------|--------------------|-------------|--------|---------|
| Constant                     | 8334.22            | 1640.70     | 5.080  | 0.000   |
| DieSizeMM                    | -163.12            | 56.43       | -2.891 | 0.016   |
| UnderfillID                  | 1405.40            | 451.18      | 3.115  | 0.011   |
| SolderComp                   | 129.64             | 87.10       | 1.488  | 0.167   |
| BallDiaMM                    | 15201.29           | 4935.58     | 3.080  | 0.012   |
| PadTypeID                    | 1177.71            | 242.40      | 4.859  | 0.001   |
| DeltaT                       | -48.05             | 6.12        | -7.857 | 0.000   |



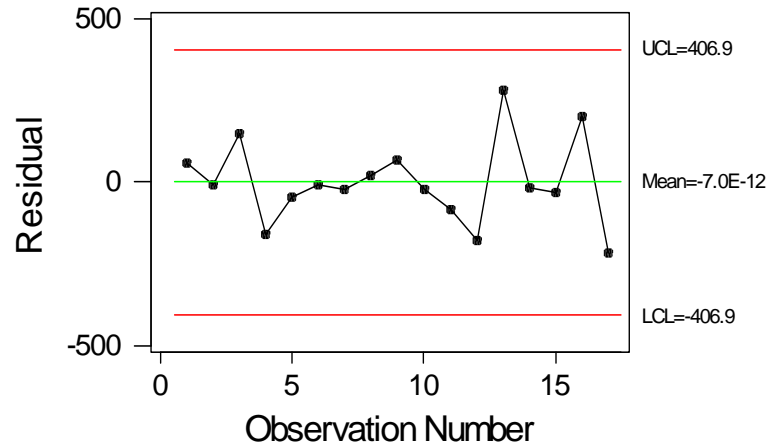
# Residual Plots for Model Diagnostics

## > *Flip-Chip*

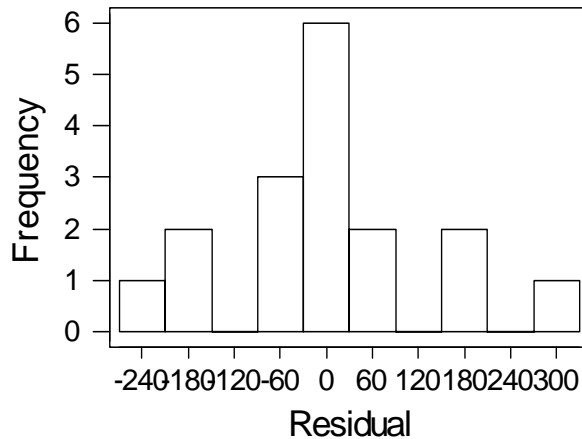
Normal Plot of Residuals



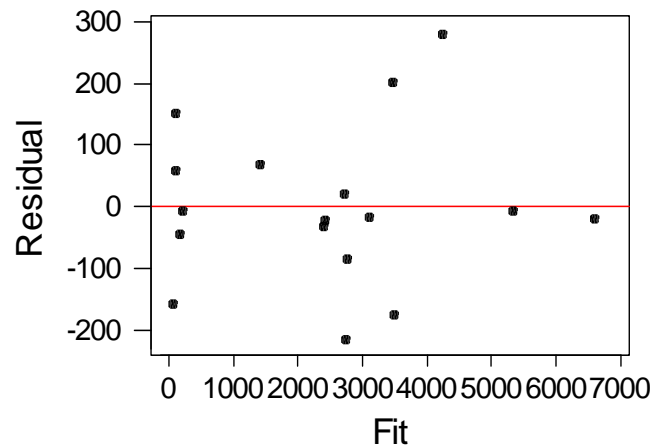
I Chart of Residuals



Histogram of Residuals



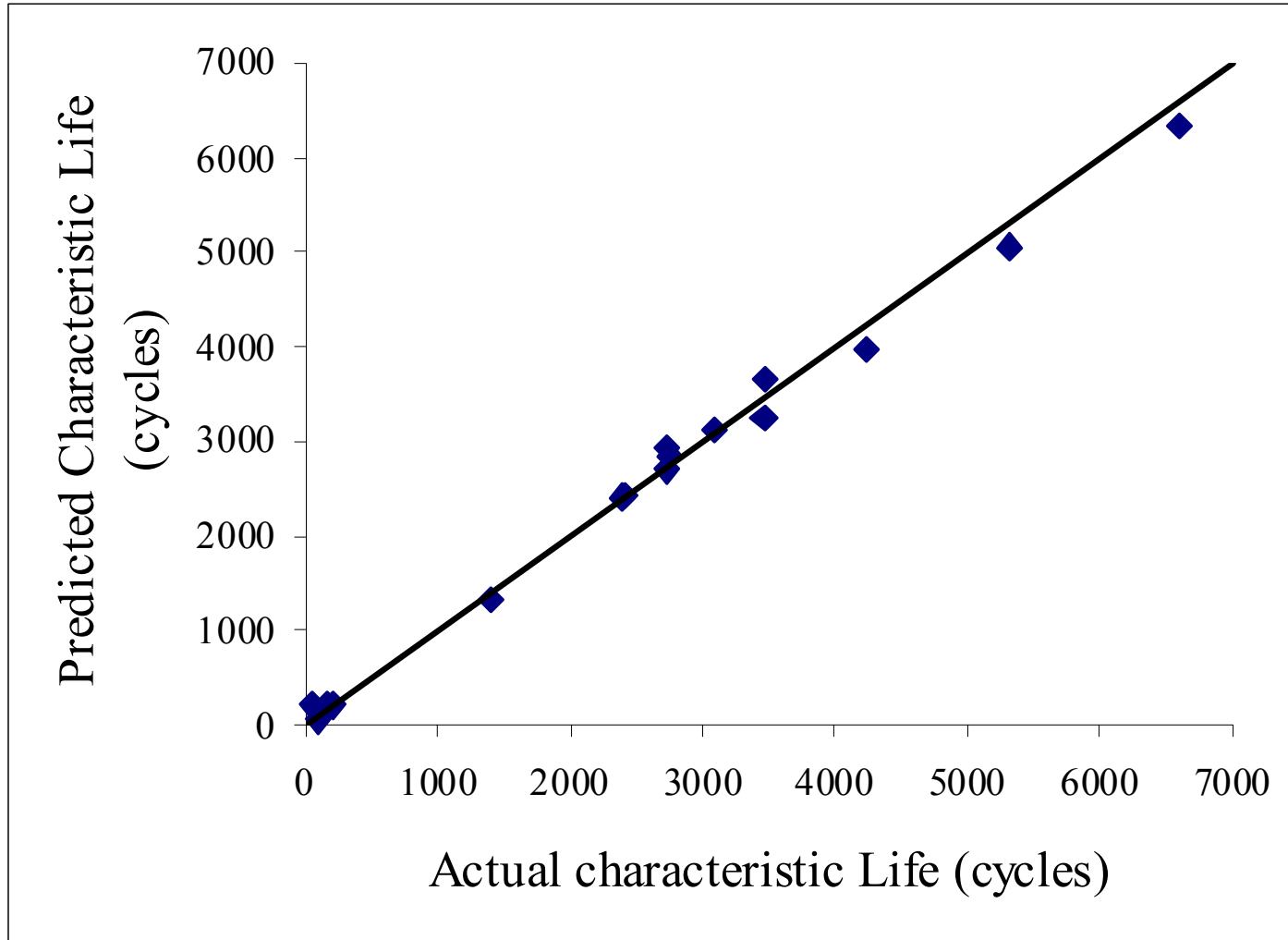
Residuals vs. Fits





# Model Correlation

## *Actual Vs Predicted, Flip-Chip*







# Failure Mechanics Models

## > *Flip-Chip*

### *Compatibility Conditions*

x-displacements at the bottom of the flip-chip and top of the substrate [Suhir 1986, 1991],

$$u_1(x) = \alpha_1 \Delta t x + \lambda_1 \int_0^x F_1(\xi) d\xi - \kappa_1 \tau_1(x) - \frac{h_1}{2} \int_0^x \frac{d\xi}{\rho(\xi)}$$

$$u_2(x) = \alpha_2 \Delta t x + \lambda_2 \int_0^x F_2(\xi) d\xi - \kappa_2 \tau_2(x) - \frac{h_2}{2} \int_0^x \frac{d\xi}{\rho(\xi)}$$

$$\tau(x) = \frac{\Delta \alpha \Delta t}{\sqrt{\lambda \kappa}} \frac{\sinh kx}{\cosh kl}$$

$$\begin{aligned} \kappa &= \kappa_1 + 2\kappa_2 + \kappa_3 & k &= \sqrt{\frac{\lambda}{\kappa}} \\ \lambda_i &= \frac{1 - \nu^2}{E_i} h_i & \kappa_i &= \frac{h_i}{3G_i} \end{aligned}$$



# Failure Mechanics Models

## > *Flip-Chip*

### *Hysteresis Loop*

Time-independent plasticity during temperature ramps modeled by parabolic relation [Knecht 1991]

Plastic flow equation with creep at dwell periods [Hall 1984, Wong 1991] used for hysteresis loop

$$\gamma_B - \gamma_A = \left( \frac{\tau_B}{\tau_P} \right)^2$$

where,

$$\tau_P (\text{Mpa}) = 348.79 - 2.07 \times T(^{\circ}\text{C})$$

o

$$\gamma_{\text{creep}} = A(T)\tau^3$$

Continue loop iteration until it converges to 0.1% accuracy



# Failure Mechanics Models

## *Life Computation (Energy-Based Models)*

Modified Morrow's Model: 
$$N_f v^{(h-1)} = \left[ \frac{C \Delta \sigma}{\Delta W} \right] \left( \frac{1}{m} \right)$$

$m = 0.7, \quad C = 1.69, \quad h = 0.9$

Darveaux's Damage Relationships: 
$$N_0 = K_1 (\Delta W)^{K_2}$$
$$\frac{da}{dN} = K_3 (\Delta W)^{K_4}$$

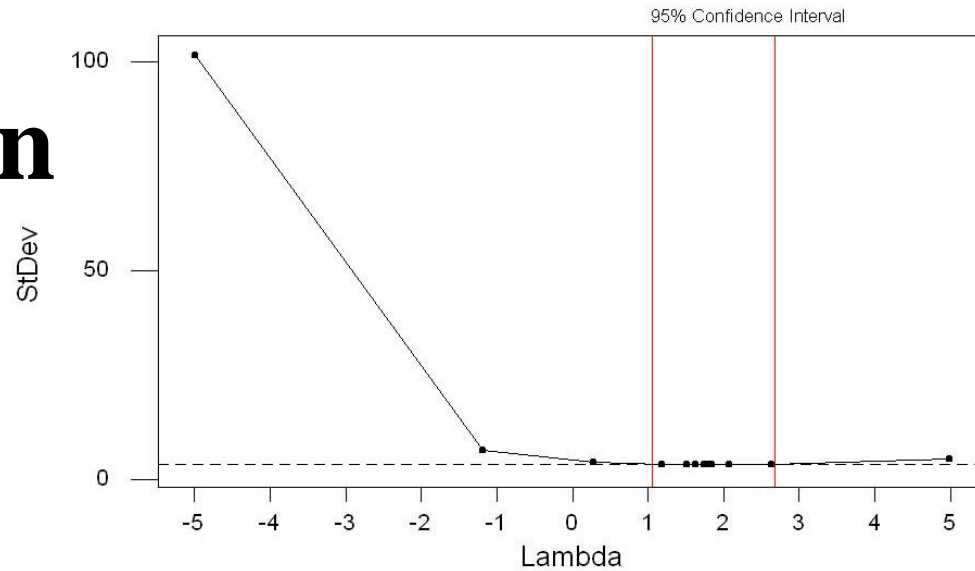
|                             | $K_1$ | $K_2$ | $K_3$                | $K_4$  |
|-----------------------------|-------|-------|----------------------|--------|
| Darveaux [1992, 1995, 2000] | 48300 | -1.64 | $3.8 \times 10^{-7}$ | 1.04   |
| Lall [2003, 2004]           | 28769 | -1.53 | $6 \times 10^{-7}$   | 0.7684 |



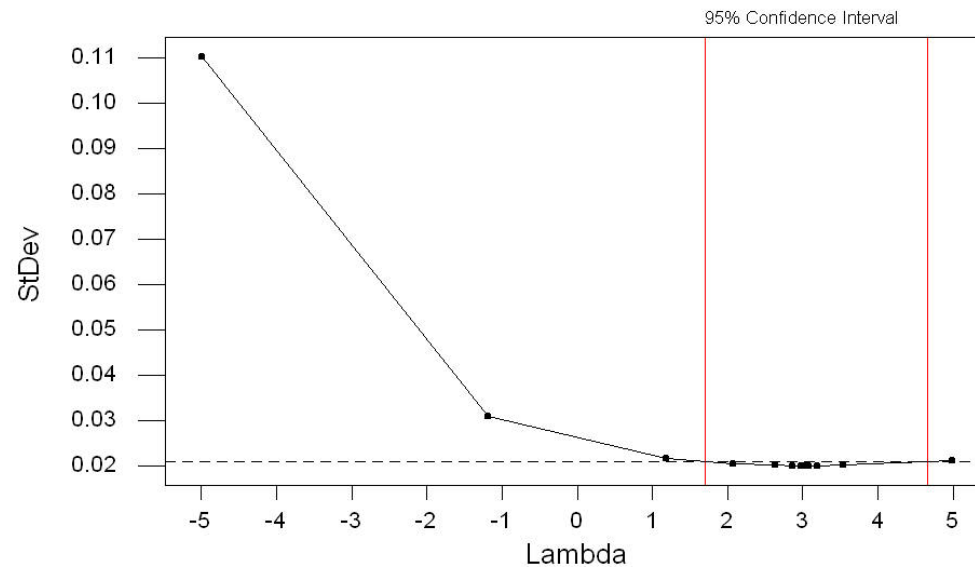
# Box-Tidwell Transformation

Determine the form of the transformation on regressor variables, and relation between the response and regressor variables.

$$E(t) = f(\xi, \beta_0, \beta_1)$$
$$= \beta_0 + \beta_1 \xi$$
$$\xi = \begin{cases} x^\alpha, & \alpha \neq 0 \\ \ln x, & \alpha = 0 \end{cases}$$



*Box-Tidwell Plot for Diagonal Length*



*Box-Tidwell Plot for Ball-Height*



# Model Validation

## *Box-Tidwell Transformation, Flip-Chip*

| Parameter       | Failure Mechanics Value | Statistical Value |
|-----------------|-------------------------|-------------------|
| Diagonal Length | 2                       | 1.798             |
| Bell Height     | 2.7                     | 3.034             |
| Ball Diameter   | 4                       | 4.89              |
| DeltaT          | 2                       | 2.7               |



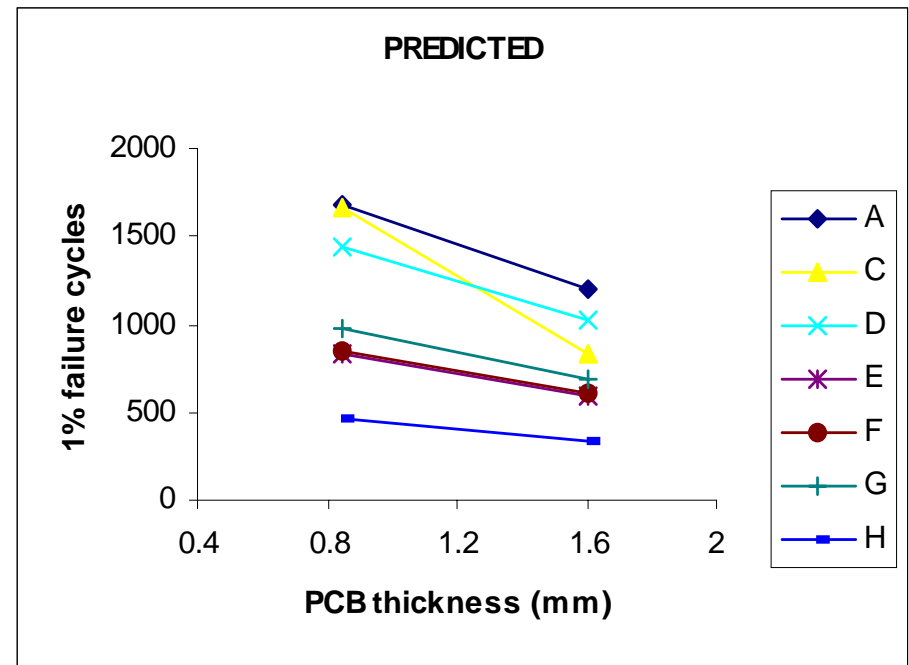
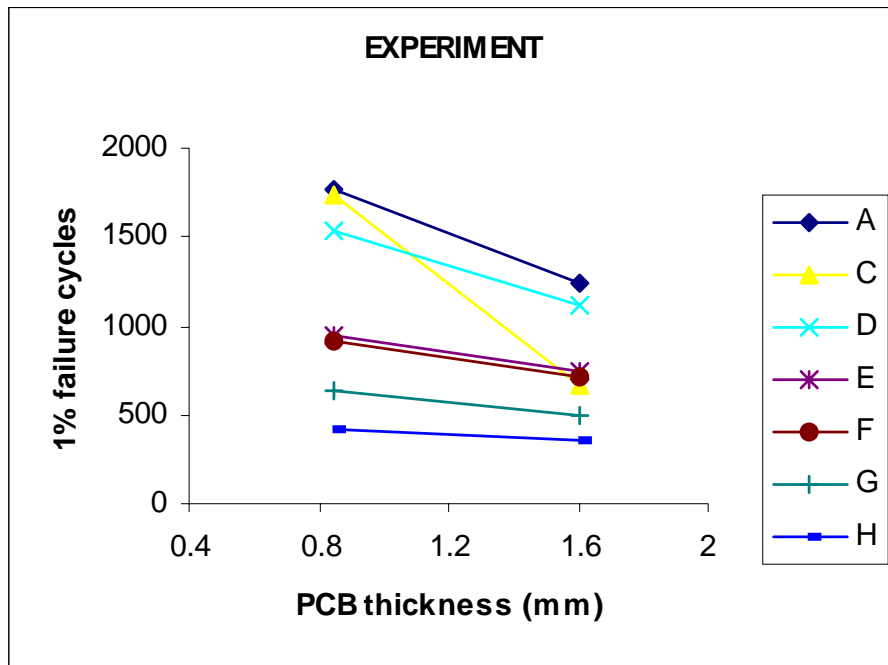
# Model Validation

Parametric variation used to validate the statistical model with the experimental data:

- Die Size
- Ball count
- Underfill / Non-underfill
- Ball Diameter
- Pad configuration (SMD/NSMD)
- Thermal cycle condition ( $\Delta T$ )



# Effect Of PCB Thickness > FlexBGAs

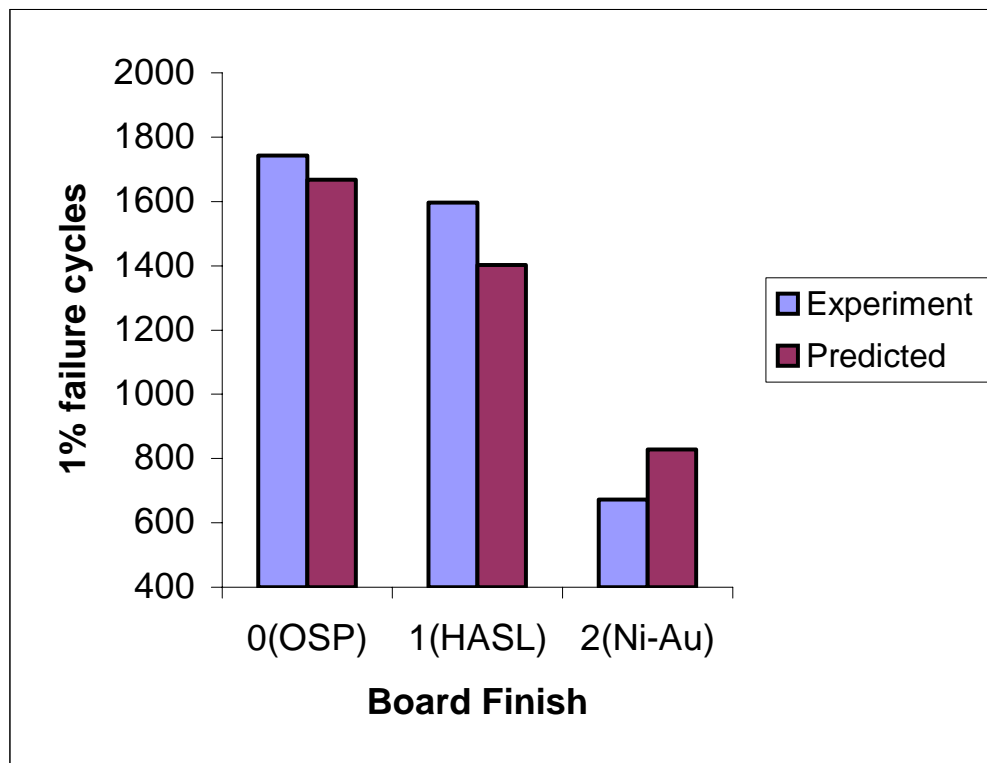


Increasing PCB thickness reduces the thermal reliability



# Effect of Board Finish

> *FlexBGA*



| Board Finish | Experimental | Model |
|--------------|--------------|-------|
| 0 (OSP)      | 1743         | 1668  |
| 1 (HASL)     | 1597         | 1403  |
| 2 (Ni-Au)    | 673          | 828   |

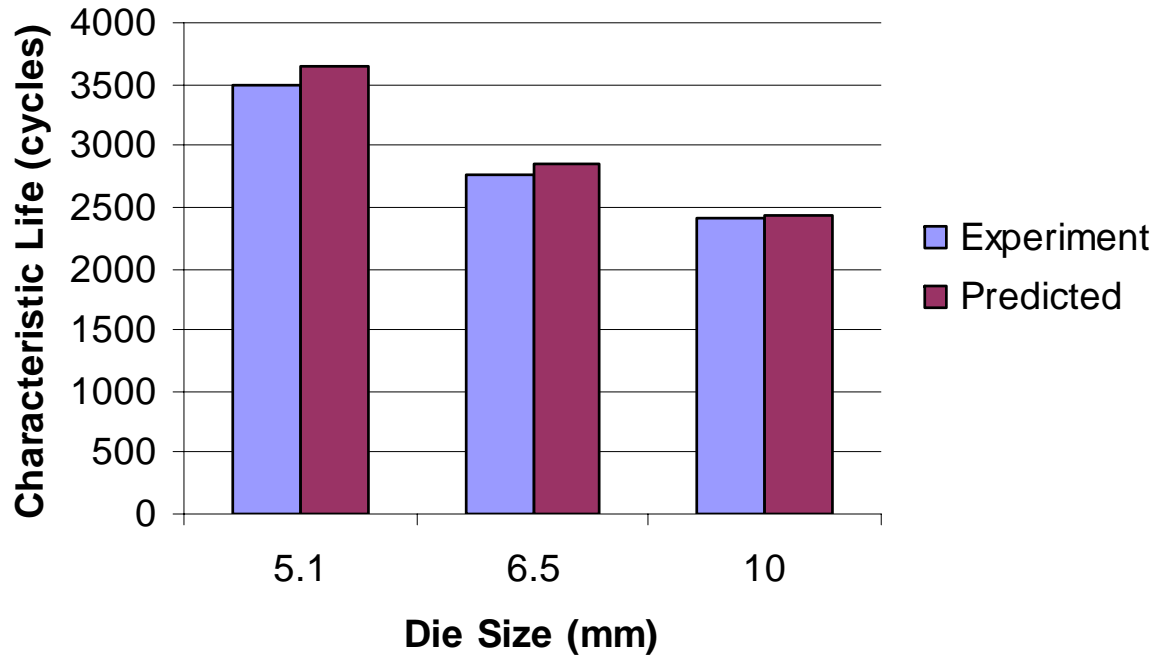
OSP Finish gives the best thermal reliability and Ni-Au Finish is worst





# Effect of Die Size

## > *Flip-Chip*



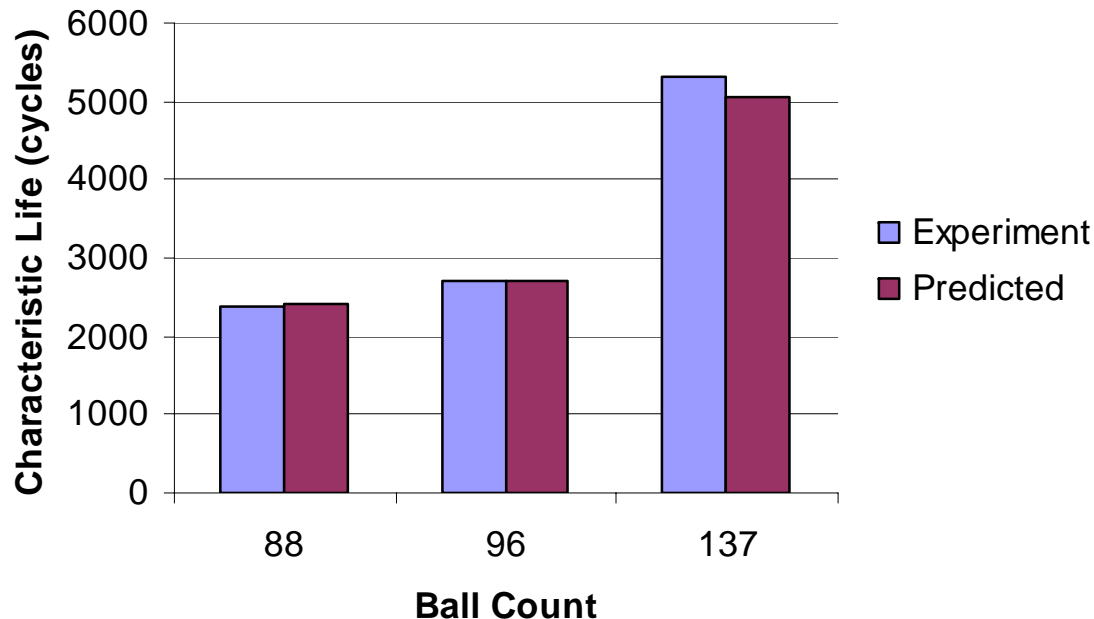
Increasing Die Size reduces the thermal reliability

| Die Size (mm) | Ball Count | Pitch (mm) | Ball Dia (mm) | ATC            | Characteristic Life (cycles) |       |
|---------------|------------|------------|---------------|----------------|------------------------------|-------|
|               |            |            |               |                | Experiment                   | Model |
| 5.1           | 88         | 0.2        | 0.112         | -25°C to 140°C | 3485                         | 3656  |
| 6.5           | 96         | 0.25       | 0.098         | -55°C to 140°C | 2764                         | 2843  |
| 10            | 184        | 0.2        | 0.126         | -25°C to 140°C | 2407                         | 2426  |



# Effect of Package I/O

## > *Flip-Chip*



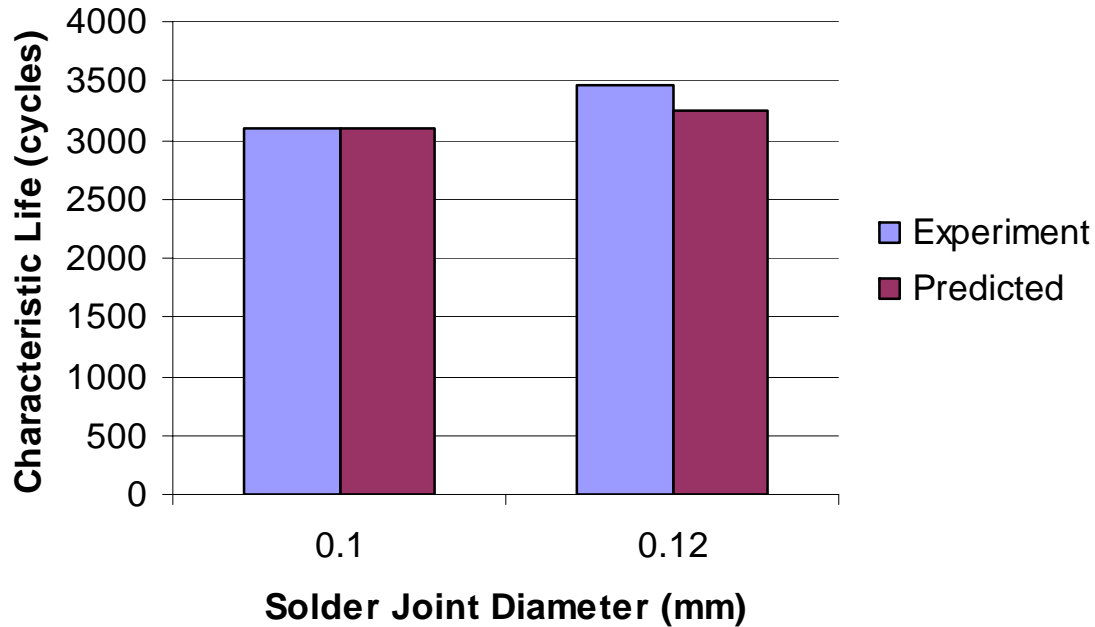
Increasing Ball Count increases the thermal reliability

| Ball Count | Die Size (mm) | Pitch (mm) | Solder Composition | ATC            | Characteristic Life (cycles) |       |
|------------|---------------|------------|--------------------|----------------|------------------------------|-------|
|            |               |            |                    |                | Experiment                   | Model |
| 88         | 5.1           | 0.2        | Sn3.5Ag            | -55°C to 140°C | 2383                         | 2410  |
| 96         | 12.6          | 0.46       | Sn37Pb             | -25°C to 140°C | 2722                         | 2697  |
| 137        | 12.6          | 0.2        | Sn0.7Cu            | 0°C to 140°C   | 5322                         | 5048  |



# Effect Of Ball Diameter

## > *Flip-Chip*



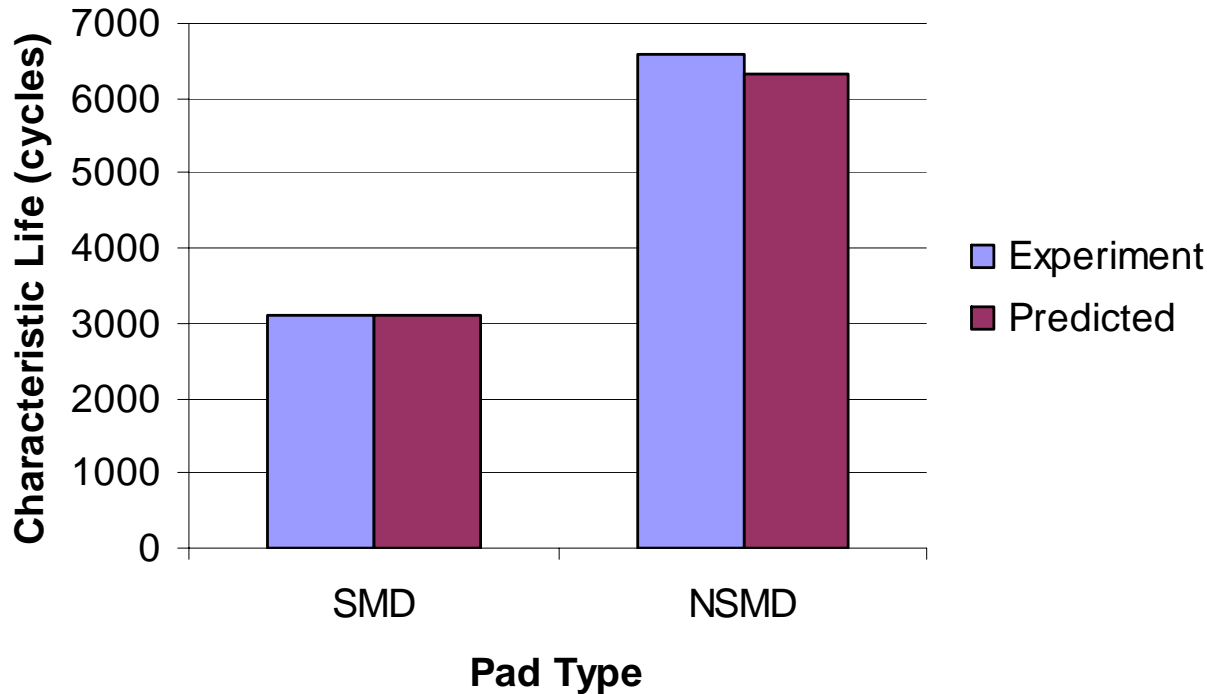
Increasing Ball Diameter  
increases the thermal reliability

| Ball Dia (mm) | Die Size (mm) | Solder Composition | ATC            | Characteristic Life (cycles) |       |
|---------------|---------------|--------------------|----------------|------------------------------|-------|
|               |               |                    |                | Experiment                   | Model |
| 0.1           | 5.1           | Sn3.5Ag            | -25°C to 140°C | 3092                         | 3104  |
| 0.12          | 5.1           | Sn3.5Ag            | -25°C to 140°C | 3456                         | 3249  |



# Effect Of Pad Configuration

## > *Flip-Chip*



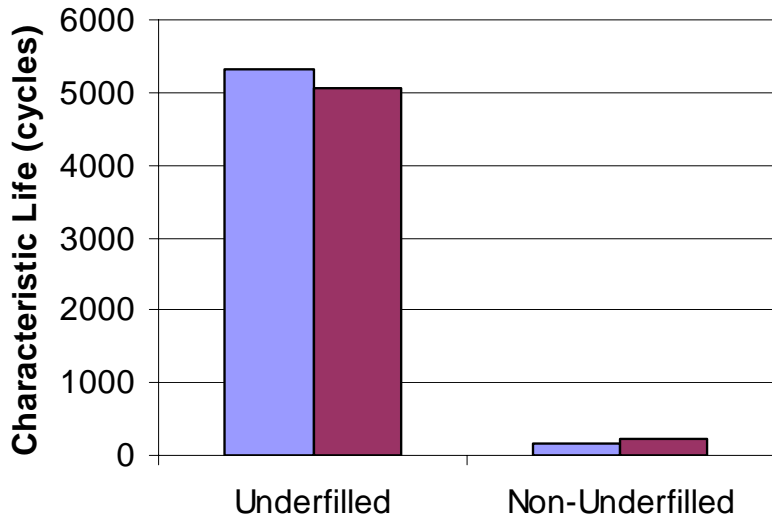
NSMD Pad configuration gives better thermal reliability than SMD Pad

| Pad Type | Die Size (mm) | Solder Composition | ATC          | Characteristic Life (cycles) |       |
|----------|---------------|--------------------|--------------|------------------------------|-------|
|          |               |                    |              | Experiment                   | Model |
| SMD      | 12.6          | Sn0.7Cu            | 0°C to 100°C | 5322                         | 5048  |
| NSMD     | 12.6          | Sn37Pb             | 0°C to 100°C | 6588                         | 6328  |

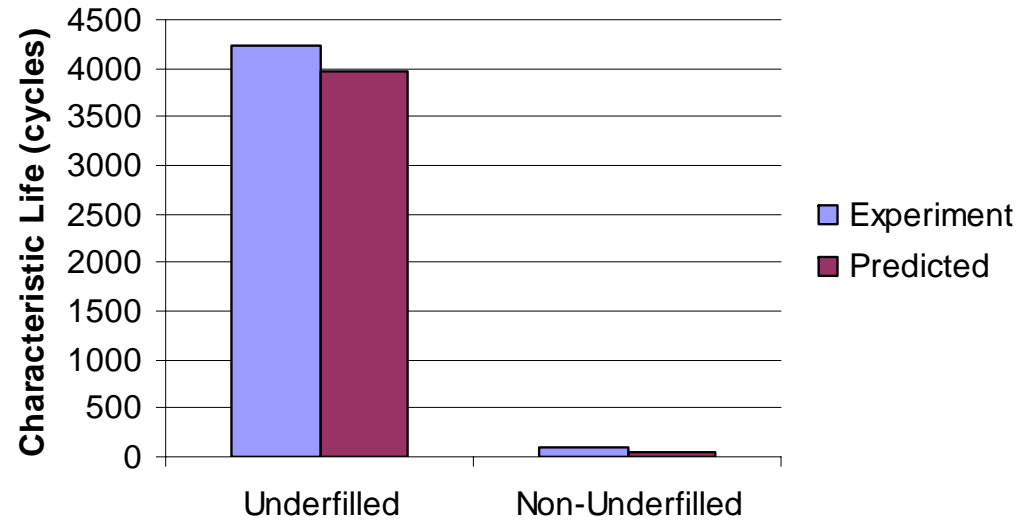


# Effect of Encapsulation

## > *Flip-Chip*



Underfill Characteristic



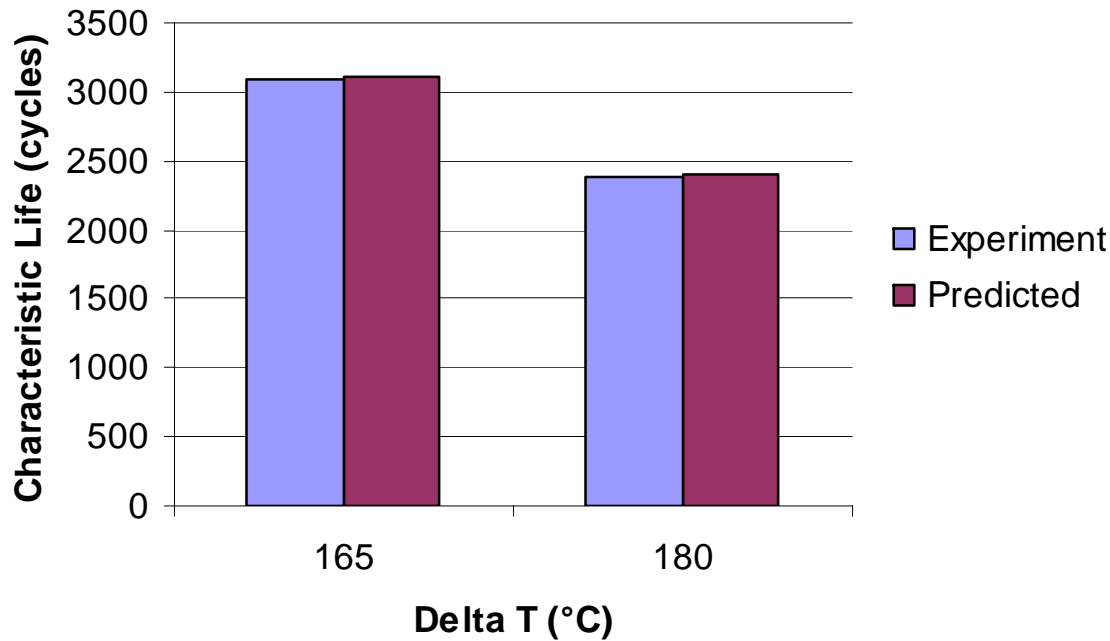
Underfill Characteristic

| Encapsulation | Die Size (mm) | Solder Composition | ATC            | Characteristic Life (cycles) |       |
|---------------|---------------|--------------------|----------------|------------------------------|-------|
|               |               |                    |                | Experiment                   | Model |
| Underfilled   | 12.6          | Sn0.7Cu            | 0°C to 110°C   | 5322                         | 5048  |
| Non-Underfill | 12.6          | Sn0.7Cu            | -40°C to 140°C | 171                          | 213   |
| Underfilled   | 5.1           | Sn4Ag0.5Cu         | -40°C to 140°C | 4243                         | 3958  |
| Non-Underfill | 12.6          | Sn4Ag0.5Cu         | -40°C to 140°C | 101                          | 41    |



# Effect of Thermal Cycling Temperature

## > *Flip-Chip*



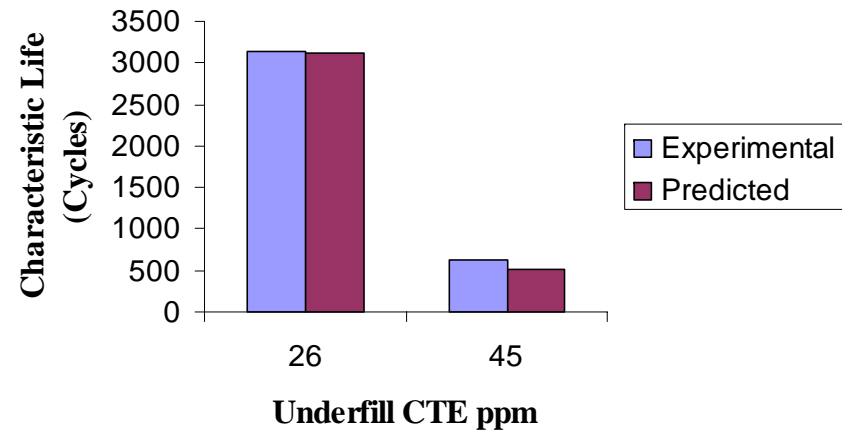
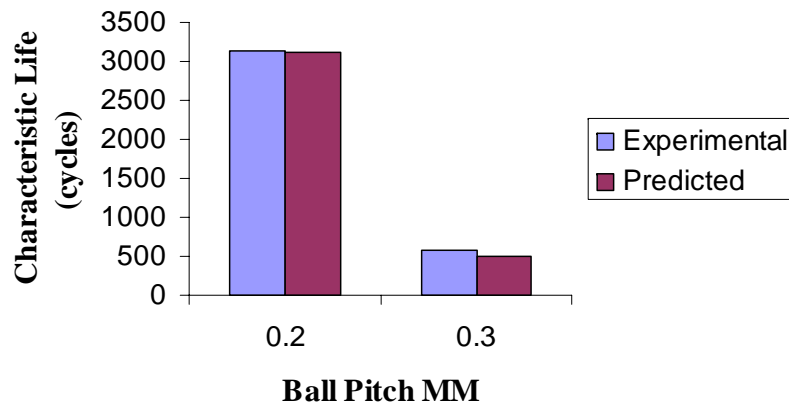
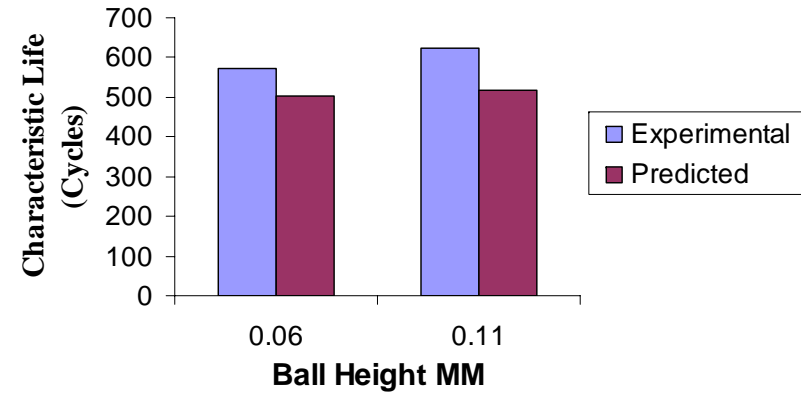
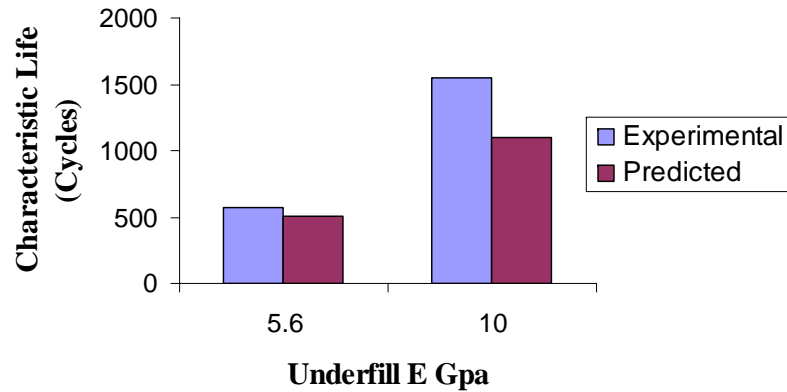
Increasing thermal cycling temperature reduces the thermal reliability

| ATC            | Cycle Time (mins) | Die Size (mm) | Ball Count | Ball Diameter (mm) | Characteristic Life (cycles) |       |
|----------------|-------------------|---------------|------------|--------------------|------------------------------|-------|
|                |                   |               |            |                    | Experiment                   | Model |
| -25°C to 140°C | 60                | 5.1           | 88         | 0.10               | 3092                         | 3104  |
| -55°C to 125°C | 17                | 5.1           | 88         | 0.12               | 2383                         | 2410  |



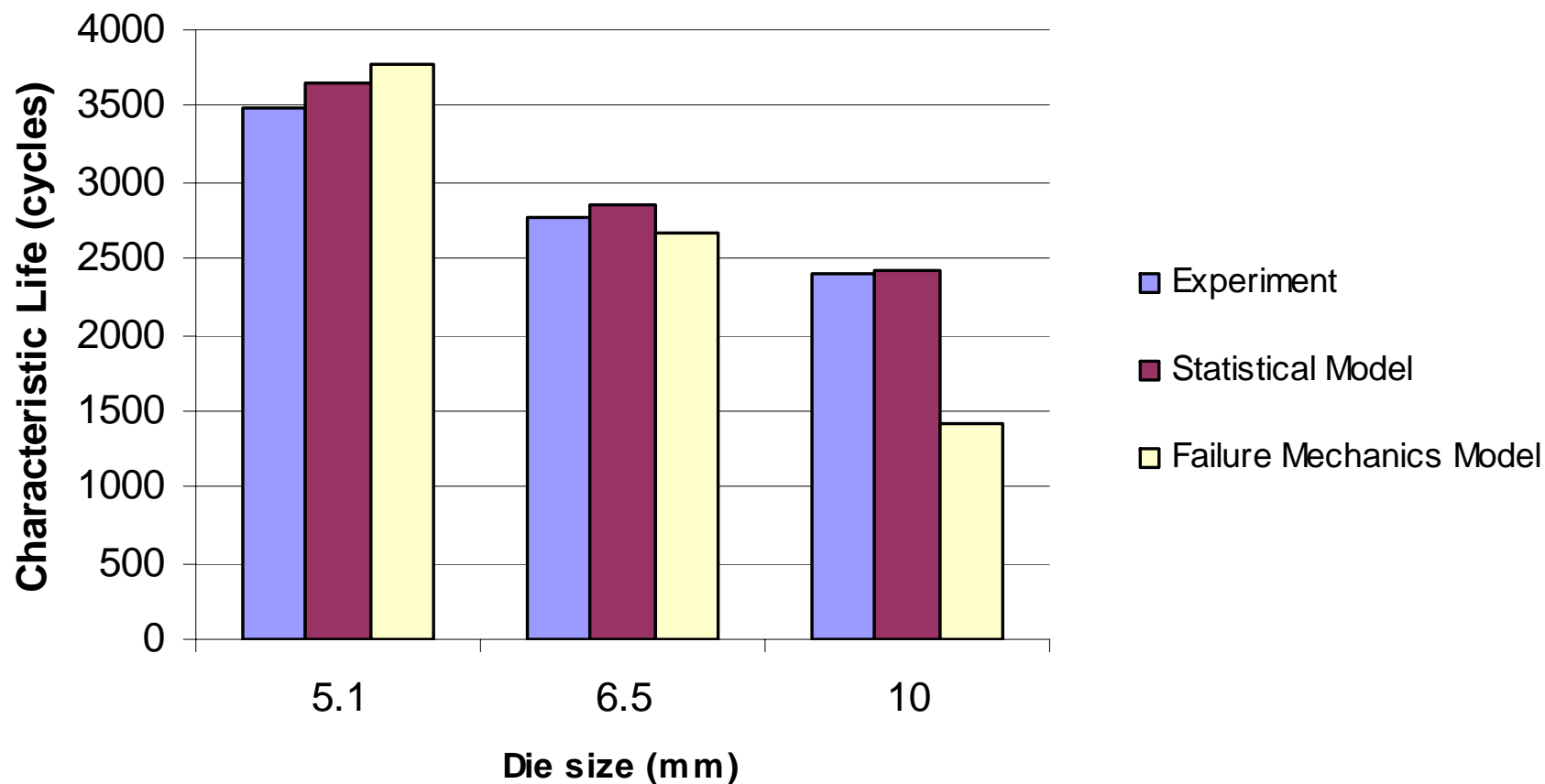
# Model Validation

## > *Flip-Chip*





# Convergence Between Model Prediction and Experimental Test Data

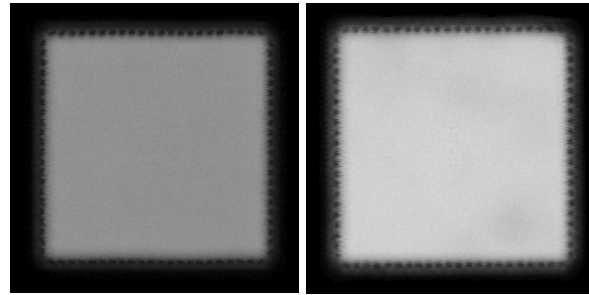






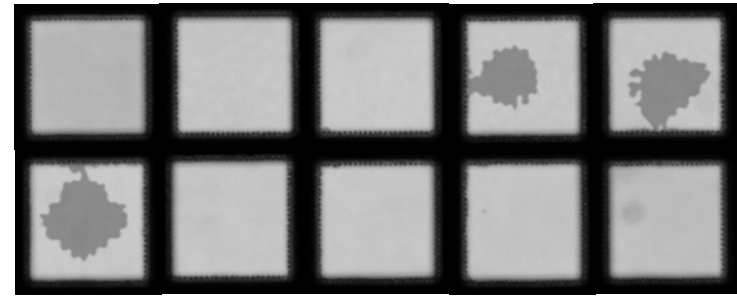
# Nano-Underfills Reliability (CSAM)

NUF-2



(a) Eutectic (b)

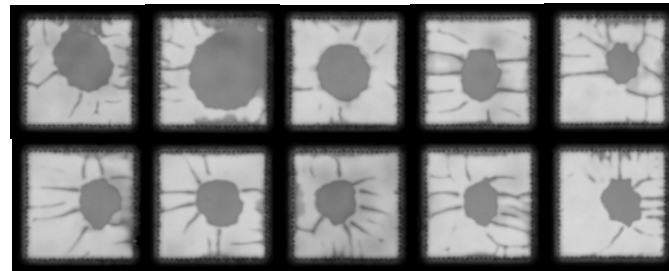
(a) As Cured, (b) After 3120 Cycles of -55°C to 125°C Thermal Shock, 100% Delamination



LF2 solder

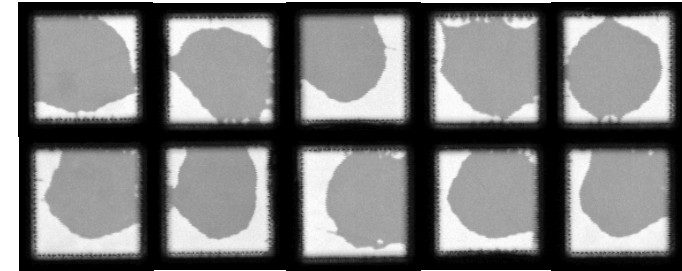
After 725 Cycles of -55°C to 150°C Thermal Shock, 70% fully Delaminated

AAB-05  
or NUF-1



Eutectic

After 3120 cycles of -55°C to 125°C thermal shock



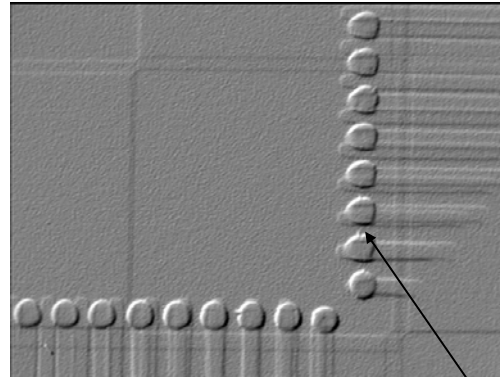
LF2 solder

After 725 cycles of -55°C to 150°C thermal shock

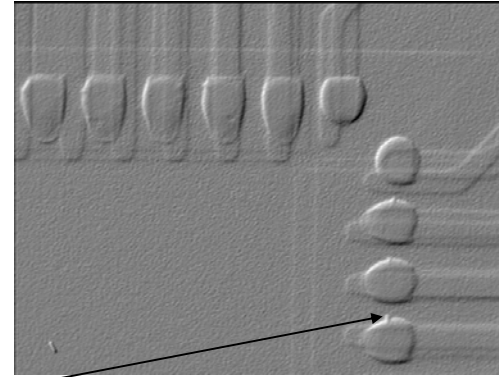


# Nano-Underfills Reliability (X-ray)

NUF-2



Eutectic



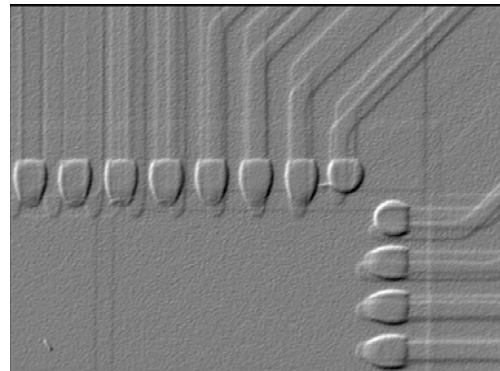
LF2 solder

Extrusion

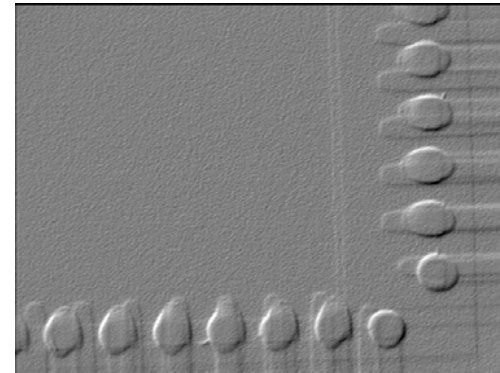
After 3120 cycles of -55°C to 125°C thermal shock

After 725 cycles of -55°C to 150°C thermal shock

AAB-05  
or NUF-1



Eutectic



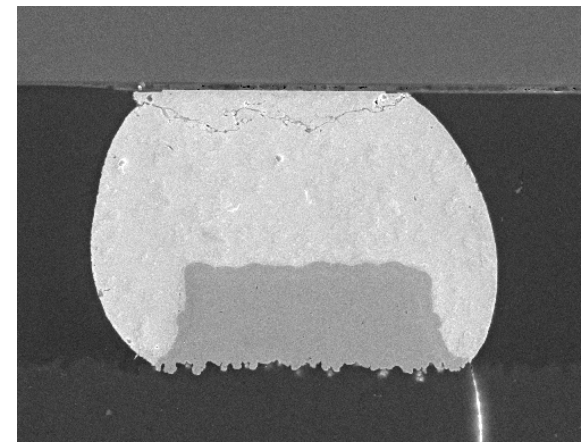
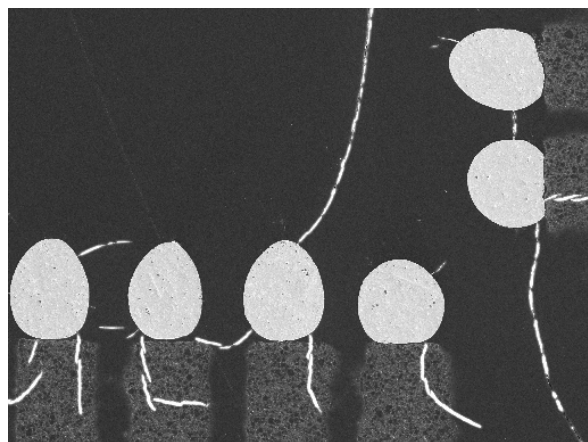
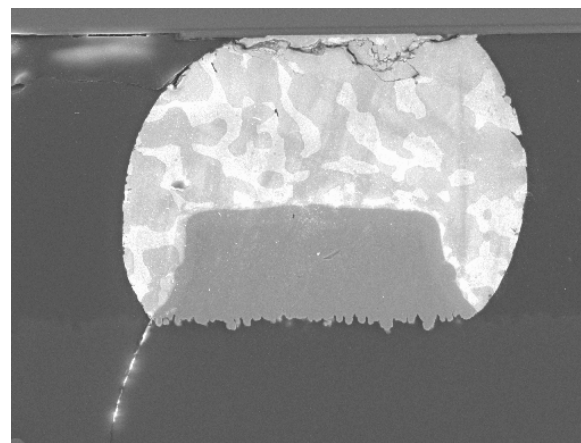
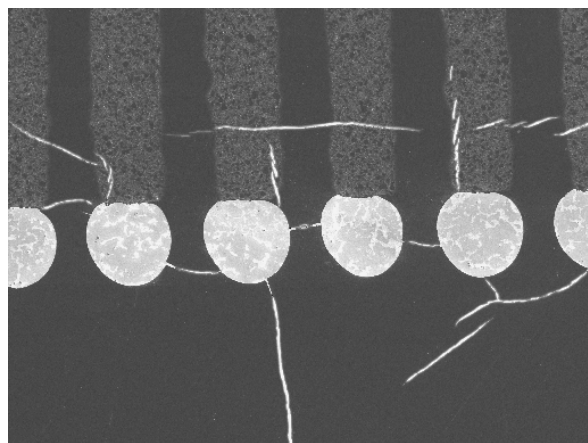
LF2 solder

After 3120 cycles of -55°C to 125°C thermal shock

After 725 cycles of -55°C to 150°C thermal shock



# Nano-Underfills Reliability (AAB-05 or NUF-1)



Underfill Crack and  
Solder Extrusion

Underfill Delamination  
and Solder Fatigue

LF2 solder

After 725 cycles  
of  $-55^{\circ}\text{C}$  to  $150^{\circ}\text{C}$   
thermal shock



# Summary

The sensitivities of reliability to design, material, architecture and environment parameters have been developed and validated with the experimental data.

The model predictions for various parametric variations show the similar trends in the effect on the reliability of the packages of various configurations.

The sensitivities developed in this paper can be used to analyze quantitatively the impact of various design parameters on the reliability of area array packages in harsh environments.